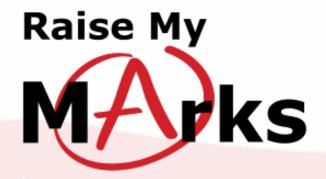
Exponential Function



RaiseMyMarks.com

2021

1

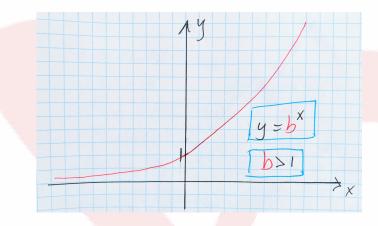
Exponentials

The exponential function is a function with the following form,

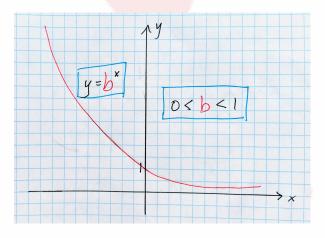
$$f(x) = b^x$$

where b is a constant real number, $b \in \mathbb{R}$, and $x \in \mathbb{R}$.

Depending on the value of b, the graph of the exponential function will change. Let's have a look. When, b > 1 we have the following graph of $y = f(x) = b^x$:



We can say that the function is "increasing". When 0 < b < 1 the graph of $y = f(x) = b^x$ has the following form:



©Raise My Marks 2021

We can say the function is "decreasing".

Notice in both situations above, the graph of the function approaches but doesn't touch or cross the x-axis. The x-axis for the above exponential functions is an *asymptote*. What is an asymptote? An *asympote* is a line that a function approaches but never reaches and thus never crosses. Let's summarize the properties of the exponential function below.

Properties of the exponential function $y = b^x$

1. b > 0

2. y-intercept
$$=1$$

3. x-axis is the horizontal aymptote.

4.
$$domain = \{x | x \in \mathbb{R}\}$$

5.
$$range = \{y \in \mathbb{R} | y > 0\}$$

- 6. $y = b^x$ is increasing if b > 1
- 7. $y = b^x$ is decreasing if 0 < b < 1

Now that we know what an exponential function looks like and have looked at the parent function $f(x) = b^x$, let's review the transformation and what they look like when applied to an exponential function.

Transformation of the exponential function $y = b^x$

$$f(x) = ab^{k(x-d)} + c$$

The parent function is b^x .

25.11.4.1.0

©Raise My Marks 2021

3 / 6

- c = vertical translation
- c < 0 vertical translation down c > 0 vertical translation up
- d =horizontal translation
- d > 0 horizontal translation left
- d < 0 horizontal translation right
- k = horizonal stretch or compression

- k > 1 is a horizonal compression
- 0 < k < 1 is a horizontal stretch
- k < 0 horizontal reflection
- a = vertical stretch or compression
- a > 1 is a vertical stretch
- 0 < a < 1 is a vertical compression
- a < 0 vertical reflection

25.11.4.1.0

©Raise My Marks 2021

Worksheet #1	Exponential Function	Pre-Calculus
Exercises		
Increasing or decreation $(a) 3^x$	sing?	
(1) (1) x		
(b) $\left(\frac{1}{4}\right)^x$		
(c) $3(4)^x + 2$		
(d) $-2^x + 1$		
(1) 7		
(e) $3\left(\frac{1}{2}\right)^x$		

Worksheet #1	Exponential Function	Pre-Calculus
(f) $-\left(\frac{1}{5}\right)^x + 3$		
(g) $2(3^x) - 1$		
(h) $-6\left(\frac{1}{3}\right)^x + 5$		
(i) $7^x - 4$		
(j) $\left(\frac{1}{8}\right)^x + 1$		
25.11.4.1.0	©Raise My Marks 2021	6 / 6