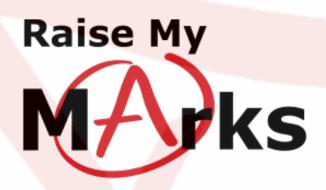
Rules of Differentiation 6



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2020



Rules of differentiation

There are a number of rules when taking the derivative of a function. B

Constant Function Rule

If f(x) = K then f'(x) = 0.

The Power Rule

If $f(x) = x^n$ then $f'(x) = nx^{n-1}$ where n is a real number, $n \in \mathbb{R}$.

Constant Multiple Rule

If f(x) = Kg(x) where K is a constant then f'(x) = Kg'(x).

The Sum Rule

If f(x) and g(x) are differentiable functions and F(x) = f(x) + g(x) then F'(x) = f'(x) + g'(x).

Difference Rule

If
$$F(x) = f(x) - g(x)$$
 then $F'(x) = f'(x) - g'(x)$

The Product Rule

If
$$F(x) = f(x)g(x)$$
 then $F'(x) = f'(x)g(x) + f(x)g'(x)$

Power Rule

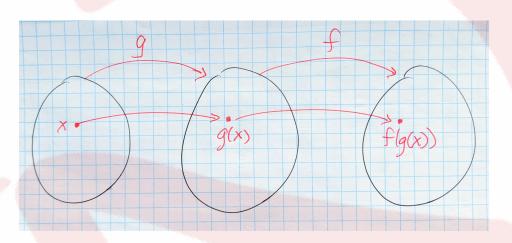
If
$$f(x) = [g(x)]^n$$
 then $f'(x) = n[g(x)]^{n-1}g'(x)$, where $n \in \mathbb{Z}$, n is an integer

The quotient Rule

If
$$F(x) = \frac{f(x)}{g(x)}$$
 then $F'(x) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$

Before we look at the chain rule for differentiation let's' look at the composition of functions. The *composition of two or more functions* can be thought of as taking the function of a function or





The domain of one function is the range of the other function. Given two functions f and g the composite function $f \circ g$ is defined by,

$$(f \circ g)(x) = f(g(x))$$

The chain rule considers the derivative of the composition of two functions.

The Chain Rule

If f and g are differentiable functions and $F(x) = f \circ g(x)$ then

$$F'(x) = f'(g(x))g'(x)$$

Using Leibniz Notation, If y = f(u), u = g(x) then,

$$\frac{dy}{dx} = \frac{dy}{du}\frac{du}{dx}.$$

Note: The power function rule is a special case of the chain rule where $f(x) = x^n$ and given some function g(x), the derivative of $F(x) = f \circ g(x) = [g(x)]^n$ is

$$f'(x) = n[g(x)]^{n-1}g'(x).$$



Exercises

Differentiate the following.

a)
$$y = (5-x)^6$$
 g) $y = \frac{1}{(x^2 - 16)^5}$

b) $y = (2x^2 + 3x - 5)^4$

h)
$$y = h = \sqrt{x^2 - 3}$$

c)
$$y = (1 - x + x^2 - x^3)^4$$

i) $y = (1 + x^{1/3})^6$

d)
$$y = [(2-x)^4 + 16]^3$$

j) $y = \frac{1}{\sqrt{x+1}}$

e)
$$y = (4x + 1)^{1/2}$$

k) $y = \left(\frac{x+2}{\sqrt[3]{x}}\right)^3$

f) $y = \sqrt{5x + 7}$

