

Rules of Differentiation 1

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Rules of differentiation

There are a number of rules when taking the derivative of a function. B

Constant Function Rule

If $f(x) = K$ then $f'(x) = 0$.

The Power Rule

If $f(x) = x^n$ then $f'(x) = nx^{n-1}$ where n is a real number, $n \in \mathbb{R}$.

Constant Multiple Rule

If $f(x) = Kg(x)$ where K is a constant then $f'(x) = Kg'(x)$.

The Sum Rule

If $f(x)$ and $g(x)$ are differentiable functions and $F(x) = f(x) + g(x)$ then $F'(x) = f'(x) + g'(x)$.

Difference Rule

If $F(x) = f(x) - g(x)$ then $F'(x) = f'(x) - g'(x)$

The Product Rule

If $F(x) = f(x)g(x)$ then $F'(x) = f'(x)g(x) + f(x)g'(x)$

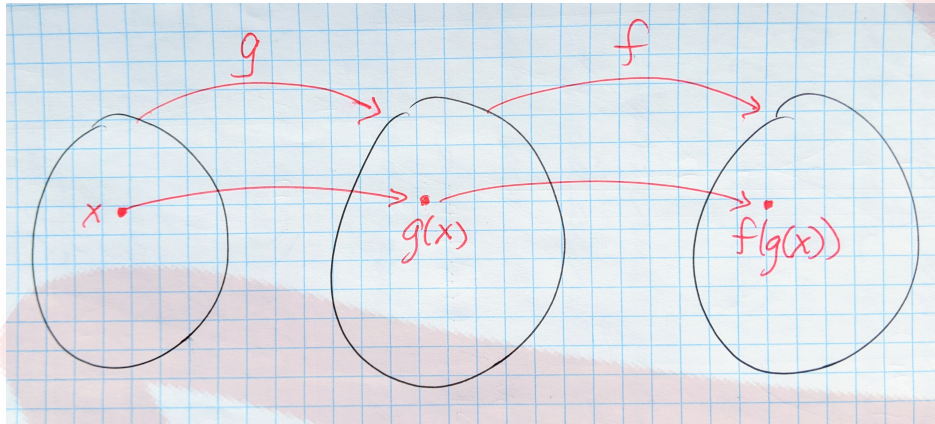
Power Rule

If $f(x) = [g(x)]^n$ then $f'(x) = n[g(x)]^{n-1}g'(x)$, where $n \in \mathbb{Z}$, n is an integer.

The quotient Rule

If $F(x) = \frac{f(x)}{g(x)}$ then $F'(x) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$

Before we look at the chain rule for differentiation let's look at the composition of functions. The *composition of two or more functions* can be thought of as taking the function of a function or



The domain of one function is the range of the other function. Given two functions f and g the composite function $f \circ g$ is defined by,

$$(f \circ g)(x) = f(g(x))$$

The **chain rule** considers the derivative of the composition of two functions.

The Chain Rule

If f and g are differentiable functions and $F(x) = f \circ g(x)$ then

$$F'(x) = f'(g(x))g'(x)$$

Using Leibniz Notation, If $y = f(u)$, $u = g(x)$ then,

$$\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$$

Note: The power function rule is a special case of the chain rule where $f(x) = x^n$ and given some function $g(x)$, the derivative of $F(x) = f \circ g(x) = [g(x)]^n$ is

$$f'(x) = n[g(x)]^{n-1}g'(x).$$

Exercises

Use the rules of differentiation to differentiate the following functions.

a) $f(x) = 4x - 7$

g) $f(x) = 6x^3 - 4x^5$

b) $f(x) = 4x^3 + 2$

h) $f(x) = (2x + 3)(x + 4)$

c) $f(x) = \frac{1}{4}x^4$

i) $f(x) = 7f(x) + 5$

d) $f(x) = (3x)^2$

j) $f(x) = \frac{4}{x^{-5}}$

e) $f(x) = \sqrt{x}$

k) $f(x) = (\sqrt{x} - 2)(3\sqrt{x} + 8)$

f) $f(x) = \frac{1}{x^2}$

l) $f(x) = \frac{x^5 - 3x^2}{2x}$

m) $f(x) = 3x^{5/3}$