## Higher Order Derivatives



RaiseMyMarks.com

2020



## **Higher Order Derivatives**

So far we have considered taking a derivative of a function, implicitly or explicitly, once only. This is the first derivative we have been considering. When we take the derivative of the first derivative, we have a second derivative; the derivative of the second derivative is the third derivative; and so on. Notation-wise we have the following:

Function	f(x) = y
1st derivative	$f'(x) = \frac{dy}{dx}$
2nd derivative	$f''(x) = \frac{d^2y}{dx^2}$
3rd derivative	$f'''(x) = \frac{d^3y}{dx^3}$

Let's consider an example.

## Example

Find the second derivative of  $f(x) = \frac{x}{1+x}$ .

Solution: We need to use the quotient rule.

$$f'(x) = \frac{1+x-x}{(1+x)^2} = \frac{1}{(1+x)^2}$$
$$f''(x) = (1+x)^{-2}$$

Now we can use the power rule.

$$f''(x) = -2(1+x)^{-3}$$

Let's fid the third derivative of the function above.

$$f'''(x) = (-2)(-3)(1+x)^{-4} = 6(1+x)^{-4}$$



## Exercises

Find the following derivatives:

a) 
$$x^2 + y^2 = 36$$
 First derivative. f)  $x^3y^3 = 144$  Second derivative

f) 
$$x^3y^3 = 144$$
 Second derivative

b) 
$$15y^2 = 2x^3$$
 Second derivative.

g) 
$$x = y + y^5$$
 Third derivative

c) 
$$3xy^2 + y^3 = 8$$
 Second derivative.

h) 
$$xy^3 - x^3y = 2$$
 First derivative

d) 
$$9x^2 - 16y^2 = -144$$
 First derivative

i) 
$$\sqrt{x} + \sqrt{y} = 5$$
 Third derivative.

e) 
$$3x^2 + 4xy^3 = 9$$
 Third derivative.