Sum and Difference of Functions



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Sum and difference of functions

Let's start by looking at the sum and difference of two functions.

Example

Let's consider an example. Let's consider the functions,

$$f(x) = x^2$$
, and $g(x) = x$

Find the sum of f and g and then graph the sum.

Sum of two functions

The sum of two functions is given by,

$$f(x) + g(x)$$

$$= x^{2} + x$$

$$= F(x)$$

where F(x) is a new function. Let's graph F(x) now.

$$F(x) = x^{2} + x, \text{ is a quaratic}$$

= $x^{2} + x + \frac{1}{4} - \frac{1}{4}$ completed square
= $\left(x + \frac{1}{2}\right)\left(x + \frac{1}{2}\right) - \frac{1}{4}$
= $\left(x + \frac{1}{2}\right)^{2} - \frac{1}{4}, \text{ vertex form of a quadratic}$

With the vertex form of the quadratic we can easily graph our function F(x).





Let's consider another example.

Example

Let's consider a difference of two functions. Let's consider the two functions,

$$f(x) = x^2$$
 and $g(x) = x + 1$

Find the difference fof f and g and graph the resulting function.

Difference of two functions

Our new function F(x) is given by,

$$F(x) = f(x) + g(x)$$

= $x^2 - (x + 1)$
= $x^2 - x + 1$, a quadratic
= $x^2 - x + \frac{1}{4} - \frac{1}{4} + 1$, completed square
= $\left(x - \frac{1}{2}\right) \left(x - \frac{1}{2}\right) + \frac{3}{4}$
= $\left(x - \frac{1}{2}\right)^2 + \frac{3}{4}$, vertex form



With the vertex form of the quadratic we can now easily graph our function F(x).



Let's consider one more example.

Example

Consider the functions,

$$f(x) = \sin x$$
 and $g(x) = \cos x$

Find the sum of f and g and then graph the sum.

Solution:

$$F(x) = f(x) + g(x) = \sin x + \cos x$$

It's probably easier to graph F(x) by either considering a table of values or looking at the graphs for sin x and cos x on the same axes and then graphically adding them.







Exercises

Given the functions $f(x) = 3x^2 + 4x - 2$ and $g(x) = -x^3 + 2x^2 + 1$ find the following functions,

a)
$$f + g$$
 f) $7f$

b) f - g

g) f + 6g + 9

c)
$$4f + 3g$$
 h) $-f + 2g - 3$

d)
$$-g+3$$
 i) $4g-3f$

e) -2g + 5f j) 2

j) 2f - 2g