# Composition of Functions 2



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## What is the composition of functions?

The composition of functions means, one function is inserted into the another function where a variable would normally go. If we consider functions f(x) and g(x), the composition of two functions f and g means, the function g is inserted into the function f as the value of x, or x = g(t) for f(x). Let's a look at an example to get a better idea of what this means and looks like.

#### Example

Let's look at the compostion of two plynomials. For example, let's consider

$$f(x) = x^2 + 3x - 1$$
 and  $g(t) = t + 1$ .

What is the composition of f and g or in notation, what is  $f \circ g$ ?

**Solution** The composition of f and g looks like,

$$f \circ g(t)$$
 or  $f(g(t))$ 

and is given by,

$$f(g(t)) = f(t+1), \text{ where } x = g(t) = t+1$$

$$= (t+1)^2 + 3(t+1) - 1$$

$$= (t^2 + 2t + 1) + (3t+3) - 1$$

$$= t^2 + 2t + 1 + 3t + 3 - 1$$

$$\therefore f(g(t)) = t^2 + 5t + 3$$

is the resulting polynomial. Let's try another example.

#### Example

Given f(x) = 2 - x and  $g(x) = \frac{2}{5-x}$  determine  $f \circ g(x)$  and  $g \circ f(x)$ .

Solution: Let's start with  $f \circ g(x)$ .

$$f(g(x)) = f\left(\frac{2}{5-x}\right) = 2 - \frac{2}{5-x} = \frac{2(5-x)-2}{5-x}$$
$$= \frac{10-2x-2}{5-x} = \frac{8-2x}{5-x}$$



Therefore,  $f(g(x)) = \frac{8-2x}{5-x}$ . Now  $g \circ f(x)$ .

$$g \circ f(x) = g(2-x) = \frac{2}{5-(2-x)} = \frac{2}{5-2+x} = \frac{2}{3+x}$$

Therefore,  $g(f(x)) = \frac{2}{3+x}$ .



### Exercises

For the following pairs of functions determine  $f \circ g(x)$  and g(f(x)).

a) 
$$f(x) = 2 - x^2$$
 and  $g(x) = 4x + 3$ 

b) 
$$f(x) = \frac{1}{2}x - x^3$$
 and  $g(x) = -4x$ 

c) 
$$f(x) = 2 - x + 2x^2$$
 and  $g(x) - 2x^2 + x^{-2}$ 

d) 
$$f(x) = \frac{1}{x-1}$$
 and  $g(x) = \frac{2}{5-x}$ 

e) 
$$f(x) = 2x + 3$$
 and  $g(x) = x - 4$ 

f) 
$$f(x) = \frac{1}{x^2}$$
 and  $g(x) = 5 - x^2$