Introduction to factoring polynomials (Single variable)



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2020



## Factoring polynomials

When you learnt how to multiply, you got so good at it that you then were asked to find the "factors" of a particular number. For example, the number 36. What are all the factors of 36? When I see this kind of problem I think, "What numbers multiply together to give 36?" Let's start with 1.

 $1 \times 36 = 36$   $2 \times 18 = 36$   $3 \times 12 = 36$   $4 \times 9 = 36$  $6 \times 6 = 36$ 

We can go even further and write 36 as the prodcut of more than 2 numbers.

 $1 \times 3 \times 2 \times 3 \times 2 = 36$  $2 \times 2 \times 9 = 36$  $3 \times 3 \times 4 = 36$  $2 \times 2 \times 3 \times 3 = 36$  $2 \times 3 \times 2 \times 3 = 36$  $2 \times 2 \times 3 \times 3 = 36$  $3 \times 3 \times 2 \times 2 = 36$ 

So the factors of 36 are,

1 and 36, 2 and 18, 3 and 12, 4 and 9, 6 and 6

So we have rewriten 36 as a product of its factors. We can do the same for polynomials. The goal when factoring polynomials is to try and rewrite the polynomials as a product of "smaller" polynomials. What does a "smaller" polynomial mean? In this case it means a polynomial of lesser or smaller "degree" than the oiginal polynomial we were given.

We'll stick to one variable in this introduction. Now, let's consider some examples.

## Example

Find all factorizations for the following polynomials:

- 1.  $x^2$
- 2.  $x^4$



- 3.  $x^2 + 2x$
- 4.  $x^3 + 2x 3x^2$
- 5.  $x^2 + x^6 + x^8 + x^{12}$

## Solution:

1.

2.

3.

4.

5.

	2 2 1
	$x^2 = x^2 \cdot 1$
	$= x \cdot x$
	— <i>w w</i>
	$x^4 = x^4 \cdot 1$
	$= x^3 \cdot x$
	$= x^3 \cdot x$ $= x^2 \cdot x^2$
	= x + x
	$\frac{x^2 + 2x}{x} = x(x+2)$
	$\omega + 2\omega = \omega(\omega + 2)$
$x^3$	$+2x - 3x^2 = x(x^2 + 2 - 3x)$

$$x^{2} + x^{6} + x^{8} + x^{12} = x^{2}(1 + x^{4} + x^{6} + x^{10})$$

Introduction to factoring polynomials (single variable) - Exercises

## Exercises

Factor each polyonmial.

1. 
$$x^2 + x^3$$

6. 
$$5x^8 - 5x^7 + 8x^7$$

2.  $3x^2 + 6x^4 - 4x^4$ 

7.  $x^3 + x^2 + x$ 

3. 
$$x(3+x^2) - x^3(3+x^2)$$
  
8.  $2x^{10} - 2x^8$ 

4. -x + 2x

9.  $x^2 + x^{10} + x^{18} + x^{26}$ 

5.  $-3x^2 - 5x + 8x^7$ 

10.  $-6x^5 + 3x^4 - x^3 + 2x^2$