Composition of Functions Evaluation



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What is the composition of functions?

The composition of functions means, one function is inserted into the another funcionn where a variable would normally go. If we consider functions f(x) and g(x), the composition of two functions f and g means, the function g is inserted into the function f as the value of x, or x = g(t) for f(x). Let's a look at an example to get a better idea of what this means and looks like.

Example

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Let's look at the composition of two plynomials. For example, let's consider

$$f(x) = x^2 + 3x - 1$$
 and $g(t) = t + 1$.

What is the composition of f and g or in notation, what is $f \circ g$?

Solution The composition of f and g looks like,

$$f \circ g(t)$$
 or $f(g(t))$

and is given by,

$$f(g(t)) = f(t+1), \text{ where } x = g(t) = t+1$$

= $(t+1)^2 + 3(t+1) - 1$
= $(t^2 + 2t + 1) + (3t+3) - 1$
= $t^2 + 2t + 1 + 3t + 3 - 1$
 $\therefore f(g(t)) = t^2 + 5t + 3$

is the resulting polynomial.

Evaluating a composite function

Let's try another example but this time we want to evaluate the composite function $f \circ g$ at a particular value for x.

Example

Given f(x) = 4x + 1 and $g(x) = -x^2$. Determine, (a) f(g(-1)) and (b) $g \circ f(0)$.



Solution:

- a) There are two ways we can apprach this exercises.
 - 1. We can first determine what the composite function f(g(x)) looks like then let x = -1 and evaluate. Let's do this and see what we get.

$$f(g(x)) = f(-x^2)$$
 where $g(x) = -x^2$
- $-4x^2 + 1$

Now we let x = -2 in our function $f(g(x)) = -4x^2 + 1$.

$$f(g(-1)) = -4(-1)^2 + 1$$

= -4 + 1
= -3

Therefore, f(g(-1)) = -3.

- 2. The second way to determine the value f(g(-1)) is to first find the value g(-1), then plug in this new value in for x in f. Let's do this.
 - i. First: $g(-1) = -(-1)^2 = -1$. ii. Second: f(g(-1)) = f(-1) = 4(-1) + 1 = -4 + 1 = -3Therefore, f(g(-1)) = -3

So, both ways gave the same answer. The second way, is much quicker.

b) Let's use the second way to find $g \circ f(0)$.

- 1. First we need to find f(0). f(0) = 4(0) = 1 = 1
- 2. Second, we need to evaluate g at f(0) = 1. So, $g(f(0)) = g(1) = -(1)^2 = -1$.

Therefore, $g \circ f(0) = -1$.



Exercises

Given $f(x) = 2 - x^2$ and g(x) = -3x, determine the following values,

a) f(-1) f) f(2)

b) $g \circ f(-1)$

g) g(f(2))

c) $f \circ g(-1)$ h) $f \circ g(-2)$)

d) g(0)

i) $g \circ g(0)$

e) f(g(0))

j) f(f(1))